

Transient modelling of permafrost dynamics in changing climate scenarios



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Motivation

- Thawing increases in a warming climate
- Storage release of water and more importantly nutrients
- May alter subsurface flow pathways
- May impact nutrient cycles
- Potential feedback effects further inducing climate change

- Need to better understand changes in hydrogeological flow pathways in response to permafrost formation and degradation
- Using a numerical model of water migration in partially frozen geological media

Mathematical / Numerical model

- Mass conservation eqns for three-phase, two-component system
 $p \rightarrow$ ice, liquid, gas
 $\beta \rightarrow$ air, water

$$\frac{\partial}{\partial t} \left[\sum_{p=l,g,i} \phi \omega_p^\beta n_p s_p \right] = - \sum_{p=l,g} \nabla \cdot [\omega_p^\beta n_p \mathbf{V}_p] + \sum_{p=l,g} \nabla \cdot [\phi \tau_p n_p D_p \nabla \omega_p^\beta] + S^\beta$$

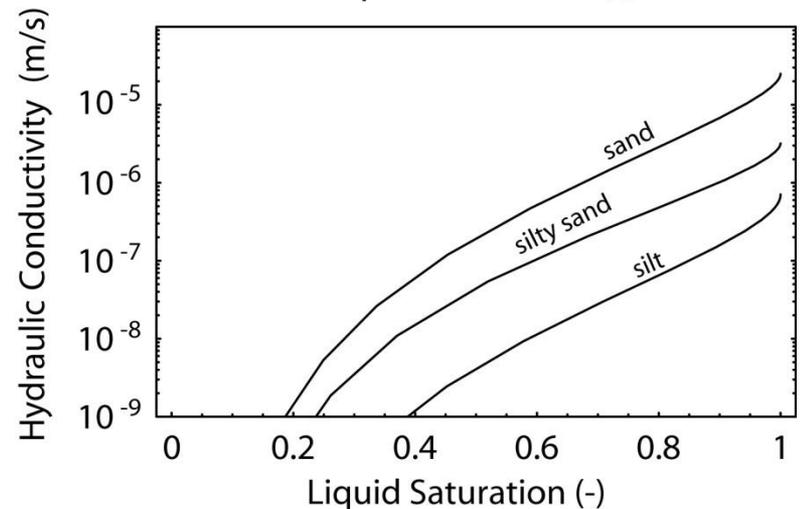
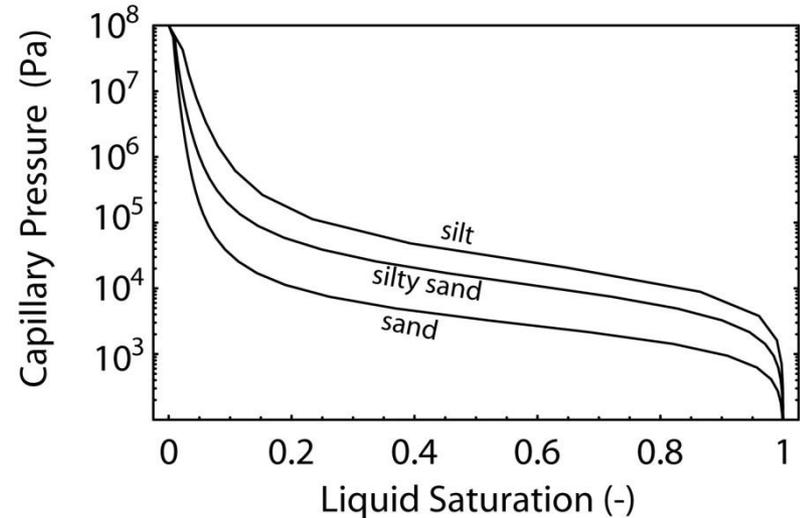
- Combined with the extended Darcy law for unsaturated flow $\mathbf{V}_p = -\frac{k_{rp} k}{\mu_p} (\nabla P_p + \rho_p g \nabla z)$

- Energy conservation eqn assumes local thermal equilibrium among the ice, liquid, gas phases and the supporting (porous) media

$$\frac{\partial}{\partial t} \left[\sum_{p=l,g,i} (\phi \rho_p s_p u_p) + (1-\phi) \rho_m u_m \right] = - \sum_{p=l,g} \nabla \cdot (\rho_p h_p \mathbf{V}_p) + \nabla \cdot [\kappa_e \nabla T] + S_E$$

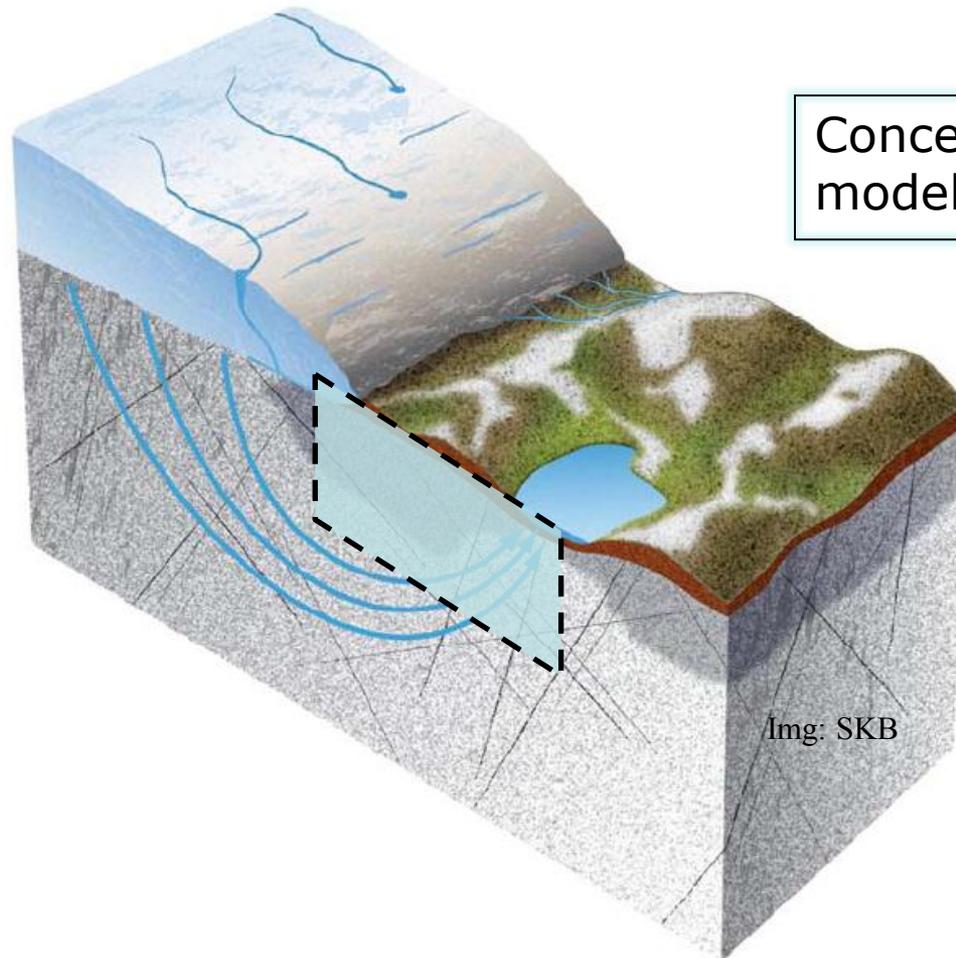
Mathematical / Numerical model

- Numerically solving the multiphase groundwater PDE coupled to heat transport
- Unfrozen water fraction and relative permeabilities obtained from unfrozen moisture retention curves
- Avoids use of empirical impedance factors
- Eg the van Genuchten and Mualem models to relate capillary pressure with phase saturation, and hydraulic conductivity to phase saturation
- Other constitutive relationships also needed to relate primary variables to secondary variables



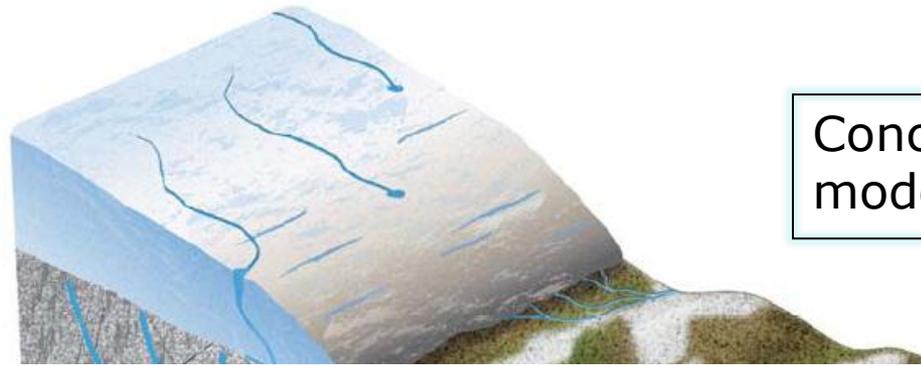
Simulation configuration

- Seasonal variability – Sinusoidally varying surface T
- Warming trends – Annually increasing mean T
Three cases – 0.5, 0.01, 0.05°C/yr over 10 years
- Heterogeneous domain – two vertically stratified textures

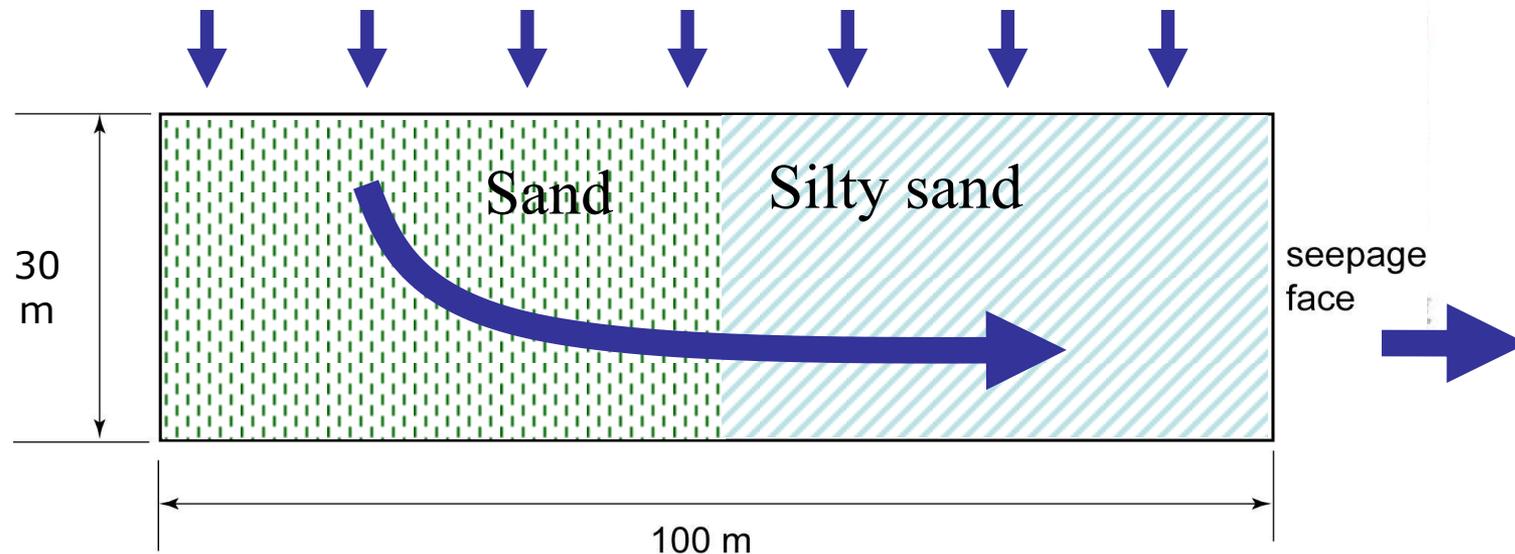


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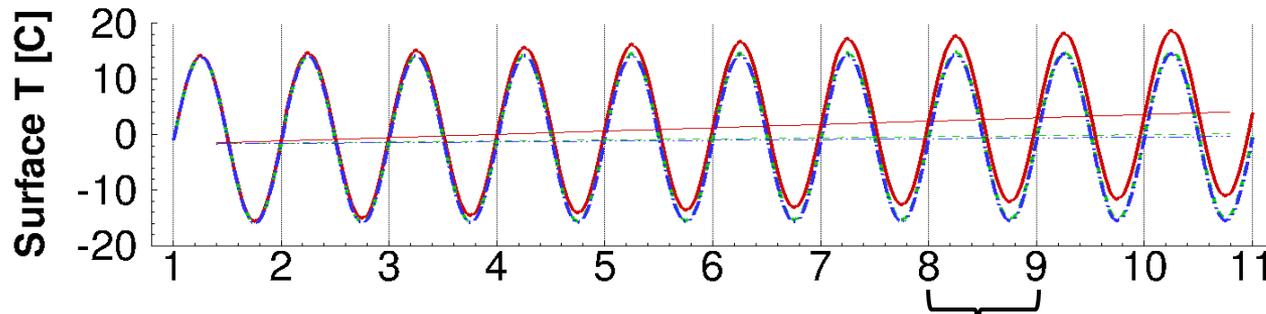


Conceptualisation of modelling approach

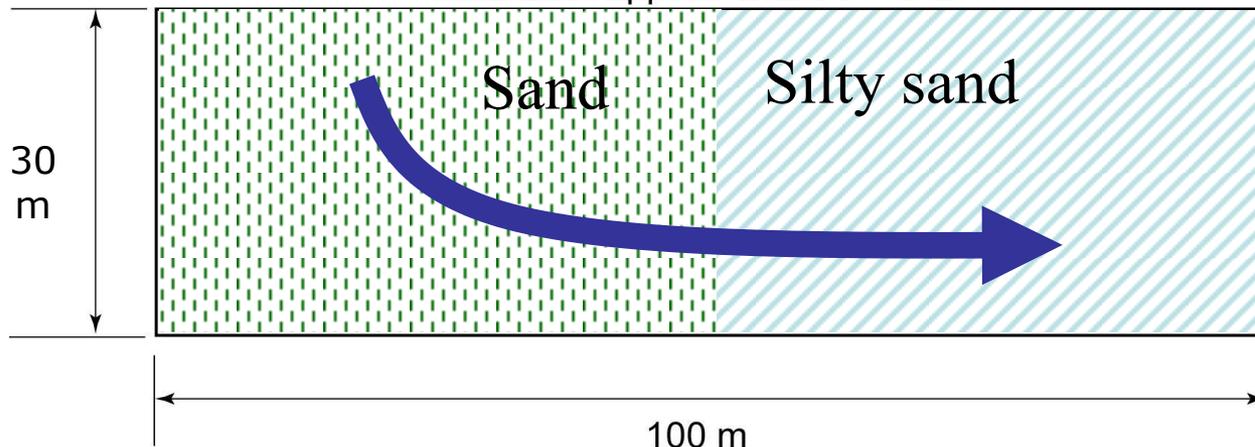


Simulation configuration

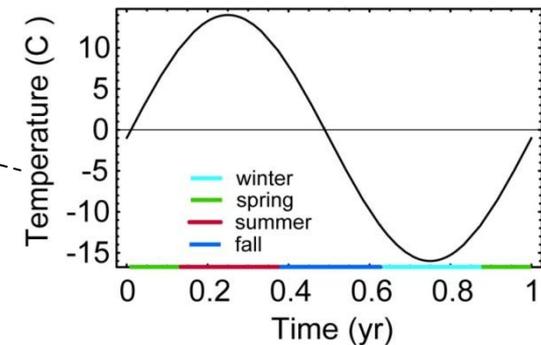
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Sinusoidally varying T
Half-amplitude = 15 C
Infiltration applied when $T > 0$ C



Annual variability in surface temperature

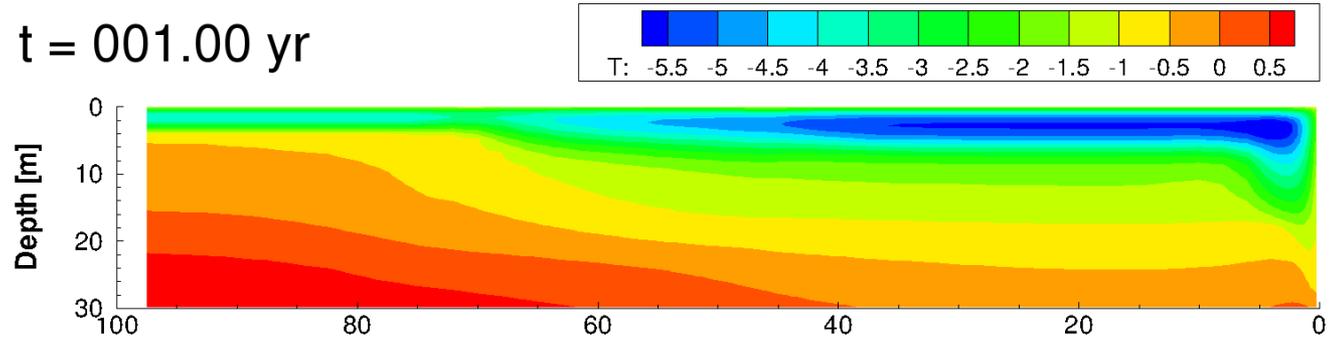


Resulting phase saturation fractions for the case of a steep warming trend

Temperature

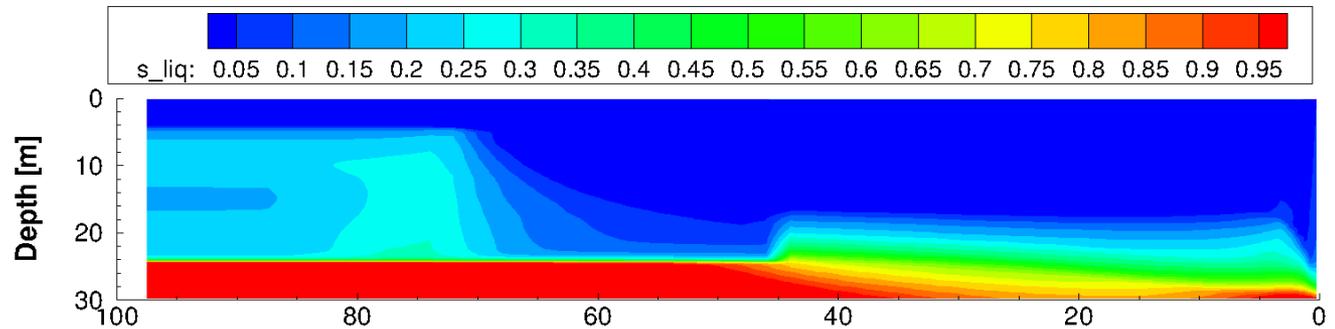
Geothermal flux at base
Seasonal T pulse

t = 001.00 yr



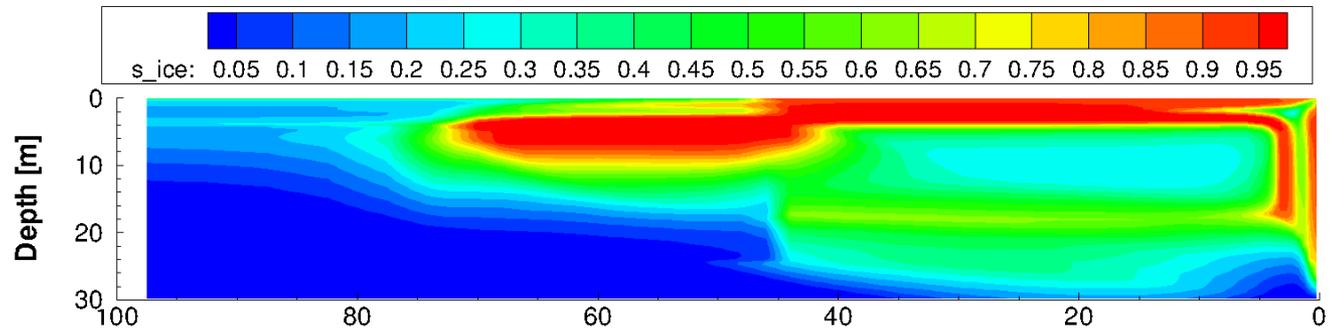
Liquid saturation

Perched layer
seasonally dependent
~Steady GW table
Bimodal flow around ice saturated regions



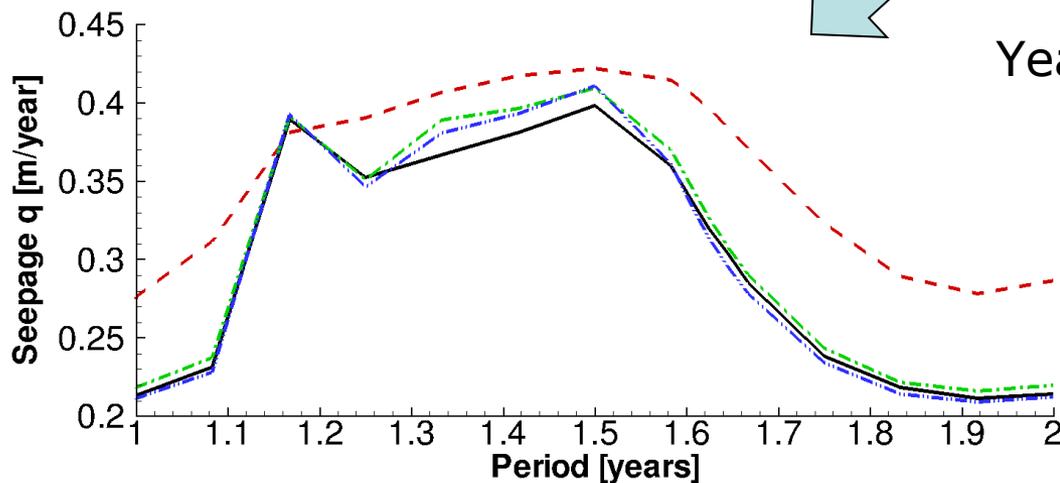
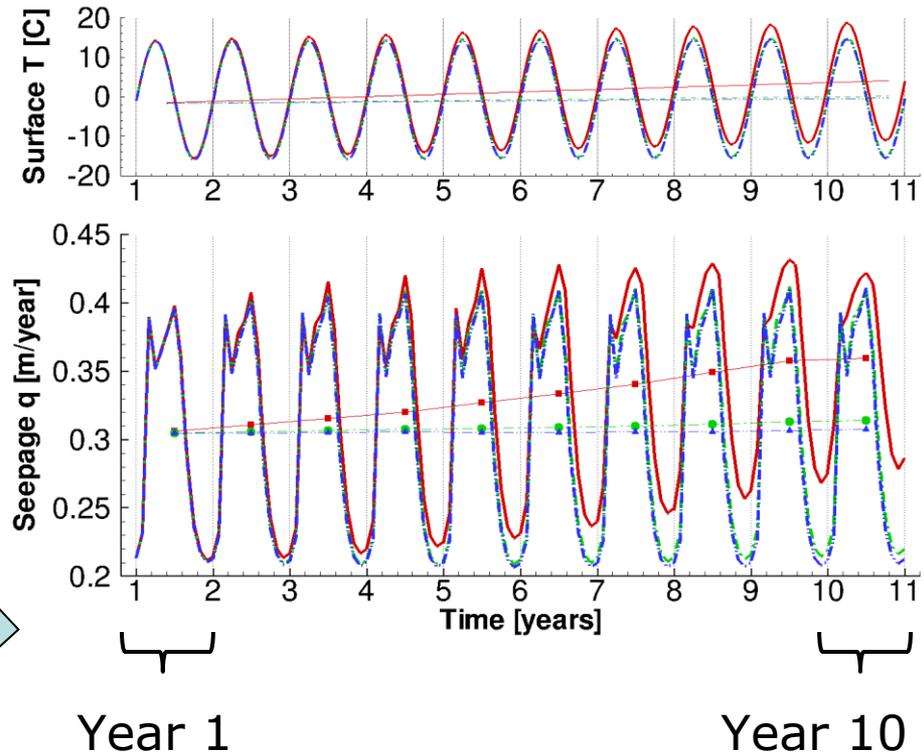
Ice saturation

Seasonally variable
Decreases with time



Implications on discharge variability along seepage face

- Decrease in seasonal variability
 - Shift in peak discharge
 - Reduction in episodic flows
- *Permafrost change may be detectable through hydrological flow signals*



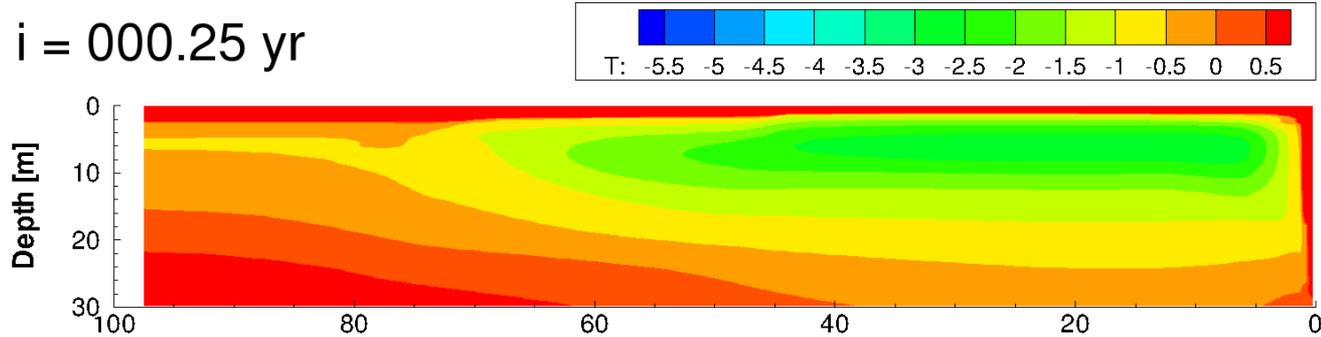
- y1
- - - y10 gradT 0.5
- · - y10 gradT 0.1
- · · - y10 gradT 0.05

Effect of a step increase in infiltration rate without a warming trend

Temperature

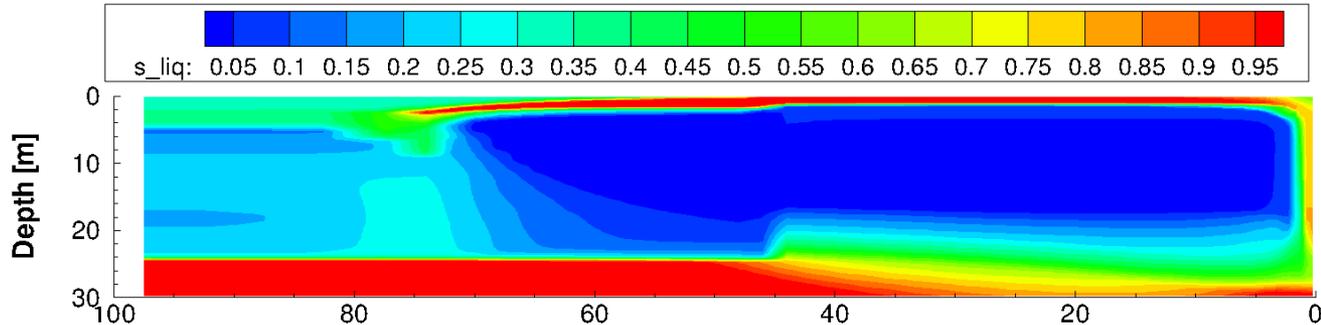
Geothermal flux at base
(Seasonal T pulse not shown)

$i = 000.25 \text{ yr}$



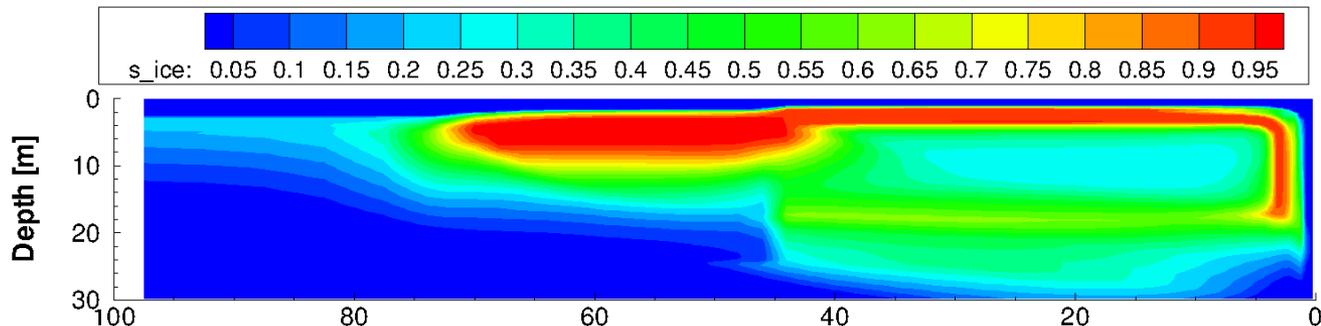
Liquid saturation

Base GW table generally increases with time



Ice saturation

Here thawing on left side due to heat from increase in infiltrating water



Summary

- Using a numerical model for multiphase, non-isothermal flow
- Can handle transient permafrost dynamics & subsurface flow
- Results show permafrost change is detectable through hydrological flow signals
- Both for warming trends and changes in infiltration
- In particular
 - Thawing in warming climate may be identified by decrease in seasonal variability of flow
 - Tendency toward episodic flows also reduced

References

- Painter, S. (2011), *Three-phase numerical model of water migration in partially frozen geological media: Model formulation, validation, and applications*, *Comput Geosciences*, 15:69–85, DOI:10.1007/s10596-010-9197-z
- Frampton, A., Painter, S.L., Lyon, S.W., Destouni, G. (2011), *Non-isothermal, three-phase simulations of near-surface flows in a model permafrost system under seasonal variability and climate change*, *J Hydrology*, 403:352–359, DOI:10.1016/j.jhydrol.2011.04.010
- Frampton, A., Painter, S.L., Sjöberg, Y., and Destouni, G. (2011). *Transient modelling of permafrost dynamics in changing climate scenarios*, 7th IEEE proceedings, Dec 5 – 8, 2011, Stockholm, Sweden (in press)